

## Section 1: Algebra

- 1.1 a.
- 1.2 all.
- 1.3  $\pm 1, \pm i$ .
- 1.4 1, 2.
- 1.5 e.g.  $x^3 + 2x + 1$ .  
(any polynomial of degree 3, for which 0, 1 and 2 are not roots (mod 3)).
- 1.6 (a)  $n$ ; (b) 0.
- 1.7 a, c.
- 1.8 b, c.
- 1.9 a, c.
- 1.10 a, c.

## Section 2: Analysis

- 2.1 (a) conditionally convergent; (b) divergent; (c) absolutely convergent.
- 2.2  $]0, 2]$ .
- 2.3 1.
- 2.4  $1/\pi$ .
- 2.5 a, c.
- 2.6 a.
- 2.7 all.
- 2.8  $8\pi i$ .
- 2.9 a, b.
- 2.10 none.

## Section 3: Topology

- 3.1 a, b.
- 3.2 b, c.
- 3.3 c.
- 3.4 c.
- 3.5 b.
- 3.6 a, c.
- 3.7 c.
- 3.8 Yes; uncountable.
- 3.9 Yes.
- 3.10 Yes; 1.

## Section 4: Applied Mathematics

4.1  $\frac{4}{3}\pi a^3$ .

4.2  $\operatorname{div} u = 0$ .

4.3 0.

4.4  $\pi^2$ .

4.5

$$\frac{1}{2}\ell^2 \left( \frac{d\theta}{dt} \right)^2 = g\ell(\cos \theta - \cos \alpha)$$

4.6  $u(x, t) = x^2 + t^2$ .

4.7  $\min z = 4$  at the point  $(8/7, 4/7)$ . (Either data can be accepted as full answer).

4.8 a, b.

4.9  $L[f](p) = a/(a^2 + p^2)$ .

4.10

$$\int_{\Omega} f \, dx + \int_{\partial\Omega} g \, dS = 0.$$

## Section 5: Miscellaneous

5.1  $\frac{n}{2} \sin \frac{2\pi}{n}$ .

5.2  $8t^4 - 8t^2 + 1$ .

5.3  $2/3$ .

5.4  $4/9$ .

5.5 all.

5.6 01.

5.7 960.

5.8 Example:  $(n + 1)! + 2, \dots, (n + 1)! + (n + 1)$ .

5.9 5.

5.10 40.