

KEY

Section 1: Algebra

- 1.1 $6!$
- 1.2 2^7
- 1.3 $N(H) = H$
- 1.4 b,c
- 1.5 c
- 1.6 Any two linearly independent elements in W .

Example:

$$\begin{bmatrix} 0 & 1 & -1 \\ -1 & 0 & 0 \\ 1 & 0 & 0 \end{bmatrix}, \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & -1 & 0 \end{bmatrix}$$

- 1.7 c
- 1.8 b,c
- 1.9 Any functional of the form $ax - ay + cz$, where $3c - a = 1$
- 1.10 a,b,c

Section 2: Analysis

- 2.1 a,c
- 2.2 a,b
- 2.3 b
- 2.4 c
- 2.5 a,b
- 2.6 b,c
- 2.7 b,c
- 2.8 a,b,c
- 2.9 $-\frac{2\pi i}{e}$
- 2.10 b,c

Section 3: Topology

- 3.1 a,b,c
- 3.2 a,c
- 3.3 b,c
- 3.4 b,c
- 3.5 b,c
- 3.6 a,c
- 3.7 a,b,c
- 3.8 a,c
- 3.9 a,b
- 3.10 a,b

Section 4: Calculus & Differential Equations

- 4.1 $-\frac{4}{\pi^2}$
- 4.2 $\frac{12\pi}{5}$
- 4.3 $\frac{3}{4}\sqrt{\pi}$
- 4.4 $y = c_1 e^{c_2 x}$
- 4.5 $y'' = g - c(y')^2$ for $t > 0$; $y(0) = y'(0) = 0$.
- 4.6 $\sqrt{\frac{g}{c}}$
- 4.7 $y' = u$; $u' = v$; $v' = v - x^2 u^2$
- 4.8 0
- 4.9 3
- 4.10 $[-(t+1), (t+1)]$

Section 5: Miscellaneous

- 5.1 a. $E \cup F$; b. F
- 5.2 $E = \bigcap_{n=1}^{\infty} \bigcup_{m=n}^{\infty} E_m$
- 5.3 $2^n(2n-1) + 1$
- 5.4 4320
- 5.5 $\frac{10}{21}$
- 5.6 Semi-major axis = 1; semi-minor axis = $\frac{1}{3}$
- 5.7 $\frac{1}{2} \log \frac{3}{2}$
- 5.8 14
- 5.9 a,b,c
- 5.10

$$\left(|a|^{\frac{3}{2}} + |b|^{\frac{3}{2}} + |c|^{\frac{3}{2}} \right)^{\frac{2}{3}}$$

Note: Please accept any correct equivalent form of the answers.