

OHAN INSTITUTE OF MATHEMA

Dedicated To Disseminating Mathematical Knowledge

CALCULUS OF VARIATION ASSIGNMENT

DECEMBER - 2014

PART - B

1. Consider the functional

$$I(y) = y^{2}(1) + \int_{0}^{1} y'^{2}(x)dx, \ y(0) = 1,$$

where $y \in C^2([0,1])$. If y extremizes J, then

1.
$$y(x) = 1 - \frac{1}{2}x^2$$
 2. $y(x) = 1 - \frac{1}{2}x$

2.
$$y(x) = 1 - \frac{1}{2}x$$

3.
$$y(x) = 1 + \frac{1}{2}x$$

3.
$$y(x) = 1 + \frac{1}{2}x$$
 4. $y(x) = 1 + \frac{1}{2}x^2$

PART - C

2. Let $y \in C^2([0,\pi])$ satisfying

$$y(0) = y(\pi) = 0$$
 and $\int_0^{\pi} y^2(x) dx = 1$

extremize the functiona

$$J(y) = \int_0^{\pi} (y'(x))^2 dx; \ y' = \frac{dy}{dx}.$$
 Then

$$1. \ \ y(x) = \sqrt{\frac{2}{\pi}} \sin x$$

1.
$$y(x) = \sqrt{\frac{2}{\pi}} \sin x$$
 2. $y(x) = -\sqrt{\frac{2}{\pi}} \sin x$

$$3. \ \ y(x) = \sqrt{\frac{2}{\pi}} \cos x$$

3.
$$y(x) = \sqrt{\frac{2}{\pi}} \cos x$$
 4. $y(x) = -\sqrt{\frac{2}{\pi}} \cos x$

JUNE - 2015

PART - C

3. The extremal of the functional

$$\int_{0}^{a} (y'^{2} - y^{2}) dx$$
 that passes through (0,0) and

 $(\alpha,0)$ has a

- 1. weak minimum if $\alpha < \pi$.
- 2. strong minimum if $\alpha < \pi$.
- 3. weak minimum if $\alpha > \pi$.
- 4. strong minimum if $\alpha > \pi$.
- **4.** The extremal of the functional $I = \int_{0}^{x_1} y^2 (y')^2 dx$

that passes through (0,0) and (x_1, y_1) is

- 1. a constant function
- 2. a linear function of x
- 3. part of parabola
- 4. part of an ellipse

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PART - B

5. The functional $I(y(x)) = \int_{0}^{b} (y^2 + y'^2 - 2y \sin x) dx$, has the following extremal with C1 and C2 as arbitrary constants.

1.
$$y = C_1 e^{2x} + C_2 e^{-2x} + \frac{1}{2} \sin x$$
.

2.
$$y = C_1 e^x + C_2 e^{-x} + \frac{1}{2} \sin x$$
.

3.
$$y = C_1 e^x + C_2 e^{-x} - \frac{1}{2} \sin x$$
.

4.
$$y = C_1 e^{2x} + C_2 e^{-2x} + \frac{1}{2} \cos x$$
.

PART - C

- 6. To show the existence of a minimizer for the functional $J[y] = \int_{0}^{b} f(x, y, y') dx$, for which there is a minimizing sequence (ϕ_n) , it is enough to have
 - 1. (φ_n) is convergent and J is continuous.
 - 2. (ϕ_n) is convergent and J is differentiable.
 - 3. (φ_n) has a convergent subsequence and J is continuous.
 - 4. (φ_n) has a convergent subsequence and J is differentiable.

JUNE - 2016

PART - B

- 7. The curve of fixed length I, that joins the points (0,0) and (1,0), lies above the x-axis, and encloses the maximum area between itself and the x-axis, is a segment of
 - 1. a straight line.
- 2. a parabola
- 3. an ellipse
- 4. a circle

PART - C

8. Let y = y(x) be the extremal of the functional

$$l[y(x)] = \int_{x}^{x_2} \sqrt{1 + \left(\frac{dy}{dx}\right)^2} dx$$
, subject to the

condition that the left end of the extremal moves along $y = x^2$, while the right end moves along x - y = 5, Then the



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- shortest distance between the parabola and the straight line is $\left(\frac{19\sqrt{2}}{8}\right)$
- slope of the extremal at (x,y) is $\left(-\frac{3}{2}\right)$.
- point $\left(\frac{3}{4},0\right)$ lies on the extremal.
- extremal is orthogonal to the curve

DECEMBER - 2016

PART - B

- **9.** If $J[y] = \int_{1}^{2} (y'^{2} + 2yy' + y^{2}) dx$, y(1) = 1 and y(2) is arbitrary then the extremal is
 - 1. e^{x-1}
- 2. e^{x+1}
- 3. e^{1-x}

PART - C

- **10.** The functional $J[y] = \int_0^1 (y'^2 + x^2) dx$ where
 - y(0)=-1 and y(1) = 1 on y=2 x 1, has
 - 1. weak minimum
 - 2. weak maximum
 - 3. strong minimum
 - 4. strong maximum
- **11.** Let y(x) be a piecewise continuously differentiable function on [0,4]. Then the functional $J[y] = \int (y'-1)^2 (y'+1)^2 dx$ attains minimum if y = y(x) is

1.
$$y = \frac{x}{2}$$
 $0 \le x \le 4$

2.
$$y = \begin{cases} -x & 0 \le x \le 1 \\ x - 2 & 1 \le x \le 4 \end{cases}$$

3.
$$y = \begin{cases} 2x & 0 \le x \le 2 \\ -x + 6 & 2 \le x \le 4 \end{cases}$$

2.
$$y = \begin{cases} -x & 0 \le x \le 1 \\ x - 2 & 1 \le x \le 4 \end{cases}$$

3. $y = \begin{cases} 2x & 0 \le x \le 2 \\ -x + 6 & 2 \le x \le 4 \end{cases}$
4. $y = \begin{cases} x & 0 \le x \le 3 \\ -x + 6 & 3 \le x \le 4 \end{cases}$

JUNE - 2017

PART - B

12. The infimum of $\int_0^1 (u'(t))^2 dt$ on the class of

 $\{u \in C^1[0,1] \text{ such that } u(0) = 0 \text{ and } \max_{u \in S^1} |u| = 1\}$

is equal to

1.0 3. 1

2. 1/2

13. Consider the functional

$$I(y(x)) = \int_{x_0}^{x_1} f(x, y) \sqrt{1 + y'^2} e^{\tan^{-1} y'} dx \text{ where}$$

 $f(x,y)\neq 0$. Let the left end of the extremal be fixed at the point $A(x_0, y_0)$ and the right end $B(x_1,y_1)$ be movable along the curve $y=\psi(x)$. Then the extremal y=y(x) intersects the curve $y=\psi(x)$ along which the boundary point $B(x_1,y_1)$ slides at an angle

- 1. $\pi/3$
- 2. $\pi/2$
- 3. $\pi/4$
- 4. $\pi/6$

DECEMBER - 2017

PART - C

Let $X = \{u \in C^1[0,1] \mid u(0)=0\}$ and let $I:X \to \mathbb{R}$ be defined as $I(u) = \int_{0}^{\infty} (u'(t)^2 - u(t)^2) dt$.

Which of the following are correct?

- 1. I is bounded below
- 2. I is not bounded below
- 3. *I* attains its infimum
- 4. *I* does not attain its infimum
- Let $I: \mathbb{C}^1[0,1] \to \mathbb{R}$ be defined as

$$I(u) = \frac{1}{2} \int_{0}^{1} (u'(t)^{2} - 4\pi^{2}u(t)^{2}) dt.$$

Let us set (P)m = inf {I (u) : $u \in C^{1}[0,1]$: u(0) = u(1) = 0}. Let $\bar{u} \in C^{1}[0,1]$ satisfy the Euler - Lagrange Equation associated with (P). Then

- 1. m= -∞ i.e., I is not bounded below
- 2. m $\in \mathbb{R}$, with I(\overline{u}) = m
- 3. m $\in \mathbb{R}$, with $I(\overline{u}) > m$
- 4. m $\in \mathbb{R}$, with $I(\overline{u}) < m$

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JUNE - 2018

PART - B

- Consider $J[y] = \int [(y')^2 + 2y] dx$ subject
 - to y(0) = 0, y(1) = 1. Then inf J[y]
- 3. is $\frac{18}{25}$
- 4. does not exist

PART - C

- **17.** The extremal the functional $J[y] = \int_{0}^{1} y'^{2}(x) dx$ subject to y(0)=0, y(1)= 1
 - and $\int_0^1 y(x) dx = 0$ is

 - 1. $3x^2 2x$ 2. $8x^3 9x^2 + 2x$
 - 3. $\frac{5}{3}x^4 \frac{2}{3}x$
 - $4.\frac{-21}{2}x^5 + 10x^4 + 4x^3 \frac{5}{2}x$
- 18. The admissible extremal for

$$J[y] = \int_0^{\log 3} [e^{-x} y'^2 + 2e^x (y' + y)] dx,$$

where y (log 3) = 1 and y(0) is free is 1. $4 - e^x$ 2. $10 - e^{2x}$ 3. $e^x - 2$ 4. $e^{2x} - 8$

DECEMBER - 2018

PART-B

19. Consider the functional

$$J[y] = \int_{0}^{2} (1 - y^{2})^{2} dx$$
 defined on {y \in C[0,2]: y

is piecewise C^1 and y(0)=y(2)=0}. Let y_e be a minimize of the above functional. Then y_{e} has

- 1. a unique corner point
- 2. two corner points
- 3. more than two corner points
- 4. no corner points

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PART-C

20. Consider the functional $J[y] = \int_0^1 [(y')^2 - (y')^4] dx$ subject to y(0)=0, y(1)=0. A broken extremal is a continuous extremal whose derivative has jump discontinuities at a finite number of

Then which of the points. following statements are true?

- There are no broken extremals and y = 0is an extremal.
- There is a unique broken extremal.
- There exist more than one and finitely many broken extremals.
- There exist infinitely many broken extremals.
- 21. The extremals of the functional

$$J[y] = \int_{0}^{1} [720x^{2}y - (y'')^{2}] dx$$
, subject to

$$y(x) = y'(0) = y(1) = 0$$
, $y'(1) = 6$, are
1. $x^6 + 2x^3 - 3x^2$ 2. $x^5 + 4x^4 - 5x^3$
3. $x^5 + x^4 - 2x^3$ 4. $x^6 + 4x^3 - 6x^2$

3.
$$x^5 + x^4 - 2x^3$$
 4. $x^6 + 4x^6$

JUNE - 19

PART - B

22. Let x*(t) be the curve which minimizes the $J(x) = \int_0^1 [x^2(t) + \dot{x}^2(t)] dt$ satisfying x(0)=0, x(1)=1. Then the value

of
$$x * \left(\frac{1}{2}\right)$$
 is

$$1. \ \frac{\sqrt{e}}{1+e}$$

$$2. \ \frac{2\sqrt{e}}{1+e}$$

3.
$$\frac{\sqrt{e}}{1+2e}$$
 4. $\frac{2\sqrt{e}}{1+2e}$

$$4. \ \frac{2\sqrt{e}}{1+2\epsilon}$$

PART - C

Let B = $\{(x, y) \in \mathbb{R}^2 | x^2 + y^2 \le 1\}$ and C = $\{(x, y) | x^2 + y^2 = 1\}$ and let f and g be continuous functions. Let u be the minimizer of the 23. functional

$$J[v] = \iint_{B} (v_x^2 + v_y^2 - 2fv) dx dy + \int_{C} (v^2 - 2gv) ds.$$

Then u is a solution of

1.
$$-\Delta u = f$$
, $\frac{\partial u}{\partial n} + u = g$

2.
$$\Delta u = f$$
, $\frac{\partial u}{\partial n} - u = g$

3.
$$-\Delta u = f$$
, $\frac{\partial u}{\partial n} = g$

4.
$$\Delta u = f$$
, $\frac{\partial u}{\partial n} = g$



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where $\frac{\partial u}{\partial x}$ denotes the directional derivative of u in the direction of the outward drawn normal at $(x, y) \in C$

24. Consider the functional

$$J[y] = \int_0^1 [(y'(x))^2 + (y'(x))^3] dx$$
, subject to $y(0) = 1$ and $y(1) = 2$. Then

- there exists an extremal $y \in C^1$ ([0, 1])\C^2 ([0, 1])
- there exists an extremal $y \in C$ ([0, 2. 1])\C¹ ([0, 1])
- every extremal y belongs to C¹ ([0, 1])
- every extremal y belongs to C² ([0, 1])

DECEMBER - 2019

PART-B

25. Let $y = \phi(x)$ be the extremizing function for

$$I(y) = \int_0^1 y^2 \left(\frac{dy}{dx}\right)^2 dx$$
, subject to

y(0) = 0, y(1) = 1. Then $\phi(1/4)$ is equal to 1. 1/2 2. 1/4

3. 1/8

PART-C

Let $y = y(x) \in C^4([0, 1])$ be an extremizing 26.

$$I(y) = \int_0^1 \left[\left(\frac{d^2 y}{dx^2} \right)^2 - 2y \right] dx, \quad \text{satisfying}$$

y(0) = 0 = y(1). Then an extremal y(x), satisfying the given conditions at 0 and 1 together with the natural boundary conditions, is given by

1.
$$\frac{x}{24}(x-1)^3$$

$$2. \ \frac{x^2}{24}(x-1)^2$$

3.
$$\frac{x}{24}(x^3-2x^2+1)$$

4.
$$\frac{x}{24}(x^3+x^2-2)$$

27. The minimum value of the functional

$$I(y) = \int_0^{\pi} \left(\frac{dy}{dx}\right)^2 dx,$$

subject to $\int_0^{\pi} y^2(x) dx = 1$, $y(0) = 0 = y(\pi)$
is equal to

1. 1/2

3. 2

2. 1 4. 1/3

JUNE - 20

PART - B

28. The extremal of the functional

$$J(y) = \int_0^1 [2(y')^2 + xy] dx, \ y(0) = 0, \ y(1)$$
$$= 1, \ y \in C^2[0, 1]$$
$$1. \ y = \frac{x^2}{12} + \frac{11x}{12}$$

2.
$$y = \frac{x^3}{3} + \frac{2x^2}{3}$$

3.
$$y = \frac{x^2}{7} + \frac{6x}{7}$$

4.
$$y = \frac{x^3}{24} + \frac{23x}{24}$$

PART - C

29. The extremal of the functional

$$J(y) = \int_0^1 e^x \sqrt{1 + (y')^2} \, dx, y \in C^2[0,1]$$
 is of the form

1.
$$y = \sec^{-1}\left(\frac{x}{c_1}\right) + c_2$$
, where c_1 and c_2

are arbitrary constants

2.
$$y = \sec^{-1}\left(\frac{x}{c_1}\right) + c_2$$
, where $|c_1| < 1$

and c2 is an arbitrary constant

3.
$$y = \tan^{-1} \left(\frac{x}{c_1}\right) + c_2$$
, where c_1 and c_2

4.
$$y = \tan^{-1} \left(\frac{x}{c_1}\right) + c_2$$
, where $|c_1| > 1$ and c_2 is an arbitrary constant

30. Consider the functional

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 $J(y) = \int_0^{\pi} ((y')^2 - ky^2) dx$ with boundary conditions y(0) = 0, $y(\pi) = 0$ Which of the following statements are

- 1. It has a unique extremal for all $k \in \mathbb{R}$
- 2. It has atmost one extremal if \sqrt{k} is not an integer
- 3. It has infinitely many extremals if \sqrt{k} is an integer
- 4. It has a unique extremal if \sqrt{k} is an

JUNE - 21

PART - B

31. Which of the following is an extremal of

> $J(y) = \int_{1}^{1} (y'^2 - 2xy) dx$ that satisfy the boundary conditions y(-1) = -1 and y(1) =

1.
$$-\frac{x^3}{5} + \frac{6x}{5}$$
 2. $-\frac{x^5}{8} + \frac{9x}{8}$

2.
$$-\frac{x^5}{8} + \frac{9x}{8}$$

3.
$$-\frac{x^3}{6} + \frac{7x}{6}$$

3.
$$-\frac{x^3}{6} + \frac{7x}{6}$$
 4. $-\frac{x^3}{7} + \frac{8x}{7}$

PART - C

32. Let $X = \{y \in C^1[0, \pi] : y(0) = 0 = y(\pi)\}$ and define $J: X \to \mathbb{R}$ by

 $J(y) = \int_{0}^{\pi} y^{2} (1 - y'^{2}) dx$. Which of the following statements are true?

- 1. y = 0 is a local minimum for J with respect to the C¹ norm on X
- 2. y = 0 is a local maximum for J with respect to the C¹ norm on X
- 3. $y \equiv 0$ is a local minimum for J with respect to the sup norm on X
- 4. $y \equiv 0$ is a local maximum for J with respect to the sup norm on X
- Let B be the unit ball in \mathbb{R}^3 centered at 33. origin. The Euler-Lagrange equation corresponding the functional to

$$I(u) = \int_{B} (1+|\nabla u|^{2})^{\frac{1}{2}} dx$$
 is

1.
$$div \left(\frac{\nabla u}{(1+|\nabla u|^2)^{\frac{1}{2}}} \right) = 0$$

$$2. \frac{\Delta u}{(1+|\nabla u|^2)^{\frac{1}{2}}} = 1$$

3.
$$|\nabla u| = 1$$

4.
$$(1+|\nabla u|^2)\Delta u = \sum_{i,j=1}^3 u_{x_i} u_{x_j} u_{x_{i}x_j}$$

JUNE - 22

PART - B

34. What is the extremal of the functional $J[y] = \int_{1}^{0} (12xy - (y')^{2}) dx$ subject to y(0) = 0 and y(-1) = 1?

1.
$$y = x^2$$

1.
$$y = x^2$$
 2. $y = \frac{2x^2 + x^4}{3}$

3.
$$y = -x^3$$

3.
$$y = -x^3$$
 4. $y = \frac{x^2 + x^4}{4}$

PART - C

35. Let $P_1 = (x_1, y_1)$ and $P_2 = (x_2, y_2)$ be two points on the xy-plane with x1 different from x_2 and $y_1 > y_2$. Consider a curve C = $\{z : z(x_1) = P_1, z(x_2) = P_2\}$. Suppose that a particle is sliding down along the curve C from the point P₁ to P₂ under the influence of gravity. Let T be the time taken to reach point P2 and g denote the gravitational constant. Which the of following statements are true?

1.
$$T = \int_{x_1}^{x_2} \sqrt{\frac{1 + (z'(x))^2}{2gz(x)}} dx$$

2.
$$T = \int_{x_1}^{x_2} \frac{\sqrt{1 + (z'(x))^2}}{2gz(x)} dx$$

- 3. T is minimized when C is a straight
- 4. The minimizer of T cannot be a straight line
- Let $X = \{u \in C^1 [0, 1] : u(0) = u(1) = 0\}$. Let 36. $\mbox{I}:\mbox{X}\rightarrow\mbox{R}\mbox{ defined as }I(u)=\int\!e^{-u'(t)^2}dt,$



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for all $\mathbf{u} \in \mathbf{X}$. Let $M = \sup_{f \in X} I[f]$ and $m = \inf_{f \in X} I[f]$. Which of the following statements are true?

1. M = 1. m = 0

2.1 = M > m > 0

3. M is attained

4. m is attained

37. If y(t) is a stationary function of

$$J[y] = \int_{-1}^{1} (1 - x^2) (y')^2 dx, y(-1) = 1, y(1) = 1$$

subject to

$$\int_{-1}^{1} y^2 = 1.$$

Which of the following statements are true?

1. y is unique

2. y is always a polynomial of even order

3. y is always a polynomial of odd order

4. No such y exists

JUNE - 23

PART - B

38. Consider the variational problem (P)

$$J(y(x)) = \int_0^1 [(y')^2 - y \mid y \mid y' + xy] dx, \quad y(0) = 0, \ y(1) = 0.$$

Which of the following statements is correct?

(1) (P) has no stationary function (extremal).

(2) $y \equiv 0$ is the only stationary function (extremal) for (P).

(P) has a unique stationary function (extremal) y not identically equal to 0.

(P) has infinitely many stationary functions (extremal).

PART - C

39. Let y(x) and z(x) be the stationary functions (extremals) of the variational problem

$$J(y(x), z(x)) = \int_0^1 [(y')^2 + (z')^2 + y'z'] dx$$

subject to y(0) = 1, y(1) = 0, z(0) = -1, z(1)

Which of the following statements are

(1) z(x) + 3y(x) = 2 for $x \in [0, 1]$.

(2) 3z(x) + y(x) = 2 for $x \in [0, 1]$.

(3) y(x) + z(x) = x for $x \in [0, 1]$.

(4) y(x) + z(x) = x for $x \in [0, 1]$.

40. Suppose y(x) is an extremal of the following functional

$$J(y(x)) = \int_0^1 (y(x)^2 - 4y(x)y'(x) + 4y'(x)^2) dx$$

subject to y(0) = 1 and y'(0) = 1/2.

Which of the following statements are

(1) y is a convex function.

(2) y is concave function.

(3) $y(x_1 + x_2) = y(x_1) y(x_2)$ for all x_1, x_2 in

(4) $y(x_1x_2) = y(x_1) + y(x_2)$ for all x_1, x_2

DECEMBER - 23

PART - B

41. The cardinality of the set of extremals of

$$J[y] = \int_0^1 (y')^2 dx,$$

$$y(0) = 1$$
, $y(1) = 6$, $\int_0^1 y \, dx = 3$

(1) 0

(2) 1(3)2

(4) countably infinite

PART - C

42. Among the curves connecting the points (1, 2) and (2, 8), let γ be the curve on which an extremal of the functional

$$J[y] = \int_{1}^{2} (1 + x^{3}y') y' dx$$

can be attained. Then which of the following points lie on the curve γ ?

(1) $(\sqrt{2},3)$

(3) $\left(\sqrt{3}, \frac{22}{3}\right)$ (4) $\left(\sqrt{3}, \frac{23}{3}\right)$

43. Define

$$S = \{ y \in C^{1}[0, \pi] : y(0) = y(\pi) = 0 \}$$

$$||f||_{\infty} = \max_{x \in [0, \pi]} |f(x)|, \text{ for all } f \in S$$

$$\mathsf{B}_0 \; (\mathsf{f}, \; \epsilon) = \{\mathsf{f} \in \mathsf{S} : ||\mathsf{f}||_{\infty} < \epsilon\}$$

$$B_1(f, \varepsilon) = \{f \in S : ||f||_{\infty} + ||f'||_{\infty} < \varepsilon\}$$

Consider the functional $J: S \to \mathbb{R}$ given by

$$J[y] = \int_0^{\pi} (1 - (y')^2) y^2 dx.$$

Then there exists $\varepsilon > 0$ such that

(1) $J[y] \le J[0]$, for all $y \in B_0$ (0, ϵ)



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(2) $J[y] \le J[0]$, for all $y \in B_1$ (0, ϵ) (3) $J[y] \ge J[0]$, for all $y \in B_0(0, \epsilon)$ (4) $J[y] \ge J[0]$, for all $y \in B_1$ (0, ϵ)	

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ANSWERS

1. (2)	2. (1,2)	3. (1,2)
4. (3)	5. (2)	6. (2,4)
7. (4)	8. (1,3)	9. (3)
10. (1,3)	11. (2,4)	12. (1)
13. (3)	14. (1,3)	15. (1)
16. (1)	17. (1)	18. (1)
19.	20. (4)	21.
22. (1)	23. (1)	24. (3,4)
25. (1)	26. (3)	27. (2)
28. (4)	29. (1)	30. (2,3)
31. (3)	32. (1)	33. (1,4)
34. (3)	35.	36. (3,4)
37.	38. (3)	39. (1,3)
40. (1,3)	41. (2)	42. (2,3)
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